

Day 2: Factoring to Solve a Quadratic

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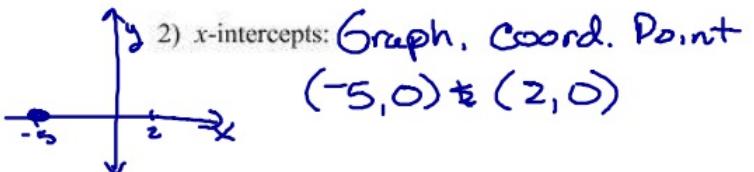
Date _____

Zeros vs x-intercepts

1) Zeros: *Equation*

$$0 =$$

$$\boxed{x : -5, 2}$$



Finding the zeros or x-intercepts of a quadratic function from Factored Form.

3) Remember the zero product property: if $ab = 0$ then $a = 0$, $b = 0$ or both a and b are 0.

This means that if $(x + 5)(x - 2) = 0$ then $x + 5 = 0$ and/or $x - 2 = 0$.

In order to use factoring to solve and graph your quadratic we do the following:

a) Change y to $y = 0$.

*When solving for zeros or x-intercepts, $y = 0$.

b) Factor the quadratic equation.

c) Solve for x .

Find the zeros of each quadratic function from Factored Form.

4) $y = (x + 3)(x - 6)$

$$0 = (\cancel{-3}+3)(\cancel{-6}-6)$$

$$0 = (\cancel{6}+3)(\cancel{6}-6)$$

$$\boxed{x : -3, 6}$$

5) $y = \left(\frac{7}{7}x - \frac{8}{7}\right)(x - 7)$

$$\boxed{x : \frac{8}{7}, 7}$$

$$\begin{aligned} &(7x - 8) \\ &\left(7\left(\frac{8}{7}\right) - 8\right) \end{aligned}$$

6) $y = \left(\frac{8}{8}x - \frac{7}{8}\right)\left(\frac{5}{8}x + \frac{4}{8}\right)$

$$\boxed{x : \frac{7}{8}, -\frac{4}{5}}$$

7) $y = (x - 7)(x - 4)$

$$\boxed{x : 7, 4}$$

8) $y = \left(\frac{5}{5}x + 2\right)(x - 5)$

$$\boxed{x : -\frac{2}{5}, 5}$$

9) $y = \left(x + 7\right)\left(x + 2\right)$

$$\boxed{x : -7, -2}$$

$$D = 25 - 45 + 20$$

Find the zeros of each quadratic function by factoring.

$$10) \quad y = x^2 - 9x + 20$$

$$(x-4)(x-5)$$

$$\begin{array}{r} 20 \\ 2 \\ \hline 4 \end{array}$$
$$\begin{array}{r} 20 \\ 10 \\ \hline 5 \end{array}$$

$$\boxed{x: 4, 5}$$

$$12) \quad y = x^2 + 3x + 2$$

$$(x+1)(x+2)$$

$$\boxed{x: -1, -2}$$

$$14) \quad y = x^2 - 7x + 12$$

$$(x-3)(x-4)$$

$$\boxed{x: 3, 4}$$

$$16) \quad y = x^2 - 8x + 7$$

$$(x-7)(x-1)$$

$$\boxed{x: 7, 1}$$

$$18) \quad y = -4x^2 + 24x$$

$$\frac{-4x^2}{-4x} = 4x$$
$$-4x(x-6)$$

$$\boxed{x: 0, 6}$$

$$20) \quad y = x^2 + 8x + 16$$

$$(x+4)(x+4)$$

$$\boxed{x: -4}$$

$$11) \quad y = x^2 + 6x + 8$$

$$(x+2)(x+4)$$

$$\boxed{x: -2, -4}$$

$$13) \quad y = x^2 - 4$$

$$(x+2)(x-2)$$

$$\boxed{x: 2, -2}$$

$$15) \quad y = x^2 + 4x + 3$$

$$(x+3)(x+1)$$

$$\boxed{x: -1, -3}$$

$$17) \quad y = 4x^2 - 16x + 16$$

$$\begin{array}{r} 4 \\ 4 \\ \hline 4 \end{array}$$
$$4(x^2 - 4x + 4)$$
$$4(x-2)(x-2)$$

$$\begin{array}{r} 4 \\ 1 \\ \hline 2 \end{array}$$

$$\boxed{x: 2}$$

$$19) \quad y = x^2 - 1$$

$$(x+1)(x-1)$$

$$\boxed{x: -1, 1}$$

$$21) \quad y = x^2 - 4$$

$$(x+2)(x-2)$$

$$\boxed{x: -2, 2}$$

$(x, 0)$

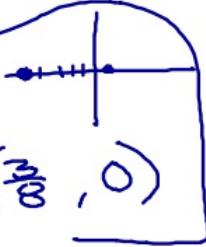
Find the x -intercepts from Factored Form.

22) $y = (x+6)(x+4)$

$(-6, 0)$ and $(-4, 0)$

24) $y = (x+5)\left(\frac{8x}{8} - \frac{3}{8}\right)$

$(-5, 0)$ and $(\frac{3}{8}, 0)$



Find the x -intercepts by factoring.

26) $y = x^2 + x - 2$
 $\begin{array}{|c|c|} \hline x & x \\ \hline -2 & 1 \\ \hline \end{array}$

$(-2, 0)$ and $(1, 0)$

23) $y = (x+7)(x-1)$

$(-7, 0)$ and $(1, 0)$

25) $y = (x+2)\left(\frac{5x}{5} + \frac{3}{5}\right)$

$(-2, 0)$ and $(-\frac{3}{5}, 0)$

27) $y = x^2 - 12x + 32$

$\begin{array}{|c|c|} \hline x & x \\ \hline -4 & 8 \\ \hline \end{array}$ $\begin{array}{r} 32 \\ \hline 2 \quad 16 \\ 4 \quad 8 \end{array}$

$(4, 0)$ and $(8, 0)$

28) $y = x^2 - 4x$
 $\begin{array}{|c|c|} \hline x & x \\ \hline 0 & 4 \\ \hline \end{array}$

$(0, 0)$ and $(4, 0)$

29) $y = x^2 - 3x + 2$
 $\begin{array}{|c|c|} \hline x & x \\ \hline 1 & 2 \\ \hline \end{array}$

$(2, 0)$ and $(1, 0)$

30) $y = x^2 - 7x - 8$
 $\begin{array}{|c|c|} \hline x & x \\ \hline -8 & 1 \\ \hline \end{array}$ $\begin{array}{r} 8 \\ \hline 1 \quad 8 \\ 2 \quad 4 \end{array}$

$X: +8, -1$ $(-8, 0), (1, 0)$

31) $y = x^2 + 3x + 2$
 $\begin{array}{|c|c|} \hline x & x \\ \hline -1 & -2 \\ \hline \end{array}$

$(-1, 0)$ and $(-2, 0)$

32) $y = x^2 - 9x + 20$
 $\begin{array}{|c|c|} \hline x & x \\ \hline 4 & 5 \\ \hline \end{array}$

$(4, 0)$ and $(5, 0)$

33) $y = x^2 + 6x + 9$
 $\begin{array}{|c|c|} \hline x & x \\ \hline -3 & -3 \\ \hline \end{array}$

$(0, 0)$ and $(-6, 0)$

34) $y = x^2 + 8x + 16$

35) $y = x^2 - 10x + 24$

